

PRIORITISING BREEDS FOR CONSERVATION USING ALLELIC DIVERSITY



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Subpopulations in conservation programmes:

1. Gene diversity or expected heterozygosity
2. Allelic diversity:
 - a. Source or variation
 - b. Selection response
 - c. Fluctuations in population size

Population with the same gene diversity and different allelic diversity (and *viceversa*):

0.5	0.5					$H = 0.5$
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0.69	0.08	0.08	0.08	0.07		$H = 0.5$
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0.7	0.04	0.04	0.04	0.04		$H = 0.5$
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0.04	0.04	0.02	0.02	0.02	
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Gene differentiation:

$$H_T = H_S + D_G$$

$$H_T = 1 - \sum_{k=1}^T \left(\sum_{i=1}^n \frac{p_{i,k}}{n} \right)^2 \quad H_S = 1 - \frac{1}{n} \sum_{i=1}^n \left(\sum_{k=1}^T p_{i,k}^2 \right)$$

$$F_{ST} = \frac{H_T - H_S}{H_T} = \frac{D_G}{H_T}$$

Allelic differentiation:

$$\mathbf{H}_T = \mathbf{H}_S + \mathbf{D}_G \quad \rightarrow \quad \mathbf{A}_T = \mathbf{A}_S + \mathbf{D}_A$$

Rarefaction (El Mousadik and Petit, 1996):

$$P_{ik} = \binom{N_i - N_{ik}}{g} / \binom{N_i}{g} \quad a_i = \sum_{k=1}^T (1 - P_{ik})$$

$$\mathbf{A}_S = \left(\frac{1}{n} \sum_{i=1}^n a_i \right) - 1$$

Allelic differentiation:

$$d_{ij} = \frac{1}{2} \sum_{k=1}^T \left[(1 - P_{ik}) P_{jk} + P_{ik} (1 - P_{jk}) \right]$$

$$D_A = \frac{1}{n^2} \left[\sum_{i,j=1}^n d_{ij} \right]$$

$$A_T = A_S + D_A = \left[\frac{1}{n} \sum_{i=1}^n \left(a_i + \frac{1}{n} \sum_{j=1}^n d_{ij} \right) \right] - 1$$

Allelic differentiation:

$$A_{ST} = \frac{A_T - A_S}{A_T} = \frac{D_A}{A_T}$$

El Mousadik and Petit (1996):

$$\rho_{ST} = 1 - \frac{(R_S - 1)}{(R_T - 1)}$$

	Alleles									
	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>e</i>	<i>f</i>	<i>g</i>	<i>h</i>	<i>i</i>	
Sub I	1	1	1	1	0	0	0	0	0	
Sub II	0	1	1	1	1	0	0	0	0	
Sub III	0	0	1	1	1	1	0	0	0	
Sub IV	0	0	0	1	1	1	1	0	0	
Sub V	0	0	0	0	1	1	1	1	0	
Sub VI	0	0	0	0	0	1	1	1	1	

	Sub I	Sub II	Sub III	Sub IV	Sub V	Sub VI
Sub I	4	5	6	7	8	8
Sub II	5	4	5	6	7	8
Sub III	6	5	4	5	6	7
Sub IV	7	6	5	4	5	6
Sub V	8	7	6	5	4	5
Sub VI	8	8	7	6	5	4

	Sub I	Sub II	Sub III	Sub IV	Sub V	Sub VI
Sub I	0	2	4	6	8	8
Sub II	2	0	2	4	6	8
Sub III	4	2	0	2	4	6
Sub IV	6	4	2	0	2	4
Sub V	8	6	4	2	0	2
Sub VI	8	8	6	4	2	0

$$A_{ST} = 0.39$$

$$\rho_{ST} = 0.63$$

	Alleles								
	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>e</i>	<i>f</i>	<i>g</i>	<i>h</i>	<i>i</i>
Sub I	1	1	1	1	0	0	0	0	0
Sub II	0	1	1	1	1	0	0	0	0
Sub III	0	0	1	1	1	1	0	0	0
Sub IV	0	0	0	1	1	1	1	0	0
Sub V	0	0	0	0	1	1	1	1	0
Sub VI	0	0	0	0	0	1	1	1	1

$$A_{ST} = 0.39$$

$$\rho_{ST} = 0.63$$

	Alleles								
	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>e</i>	<i>f</i>	<i>g</i>	<i>h</i>	<i>i</i>
Sub I	1	1	1	1	1	1	1	1	1
Sub II	1	1	1	0	0	0	0	0	0
Sub III	1	1	1	0	0	0	0	0	0
Sub IV	1	1	1	0	0	0	0	0	0
Sub V	1	1	1	0	0	0	0	0	0
Sub VI	1	1	1	0	0	0	0	0	0

$$A_{ST} = 0.22$$

$$\rho_{ST} = 0.63$$

Subpopulation	Allele						Statistic
	1	2	3	4	5	6	
I	0.2	0.3	0.5				$F_{ST} = 0.22$
II		0.2	0.3	0.1	0.1	0.3	$A_{ST} = 0.39$
III	0.5	0.5					$\rho_{ST} = 0.55$
IV				0.3	0.3	0.4	

Subpopulation	Allelic Richness			Allelic Diversity		
	Total	Within	Between	Total	Within	Between
No rarefaction						
I	0.0	-1.7	+1.7	+0.6	-2.3	+2.8
II	0.0	+11.7	-11.7	+18.6	+15.8	+2.8
III	0.0	-8.3	+8.3	-8.5	-11.3	+2.8
IV	0.0	-1.7	+1.7	+6.6	-2.3	+8.9
$g = 10$						
I	-0.9	-1.1	+0.2	0.0	-1.2	+1.2
II	+1.3	+10.3	-8.9	+14.3	+11.5	+2.8
III	+2.4	-8.7	+11.1	-8.4	-9.8	+1.3
IV	+19.5	-0.5	+20.0	+10.3	-0.6	+10.9

Petit et al. (1998):

Argan tree:

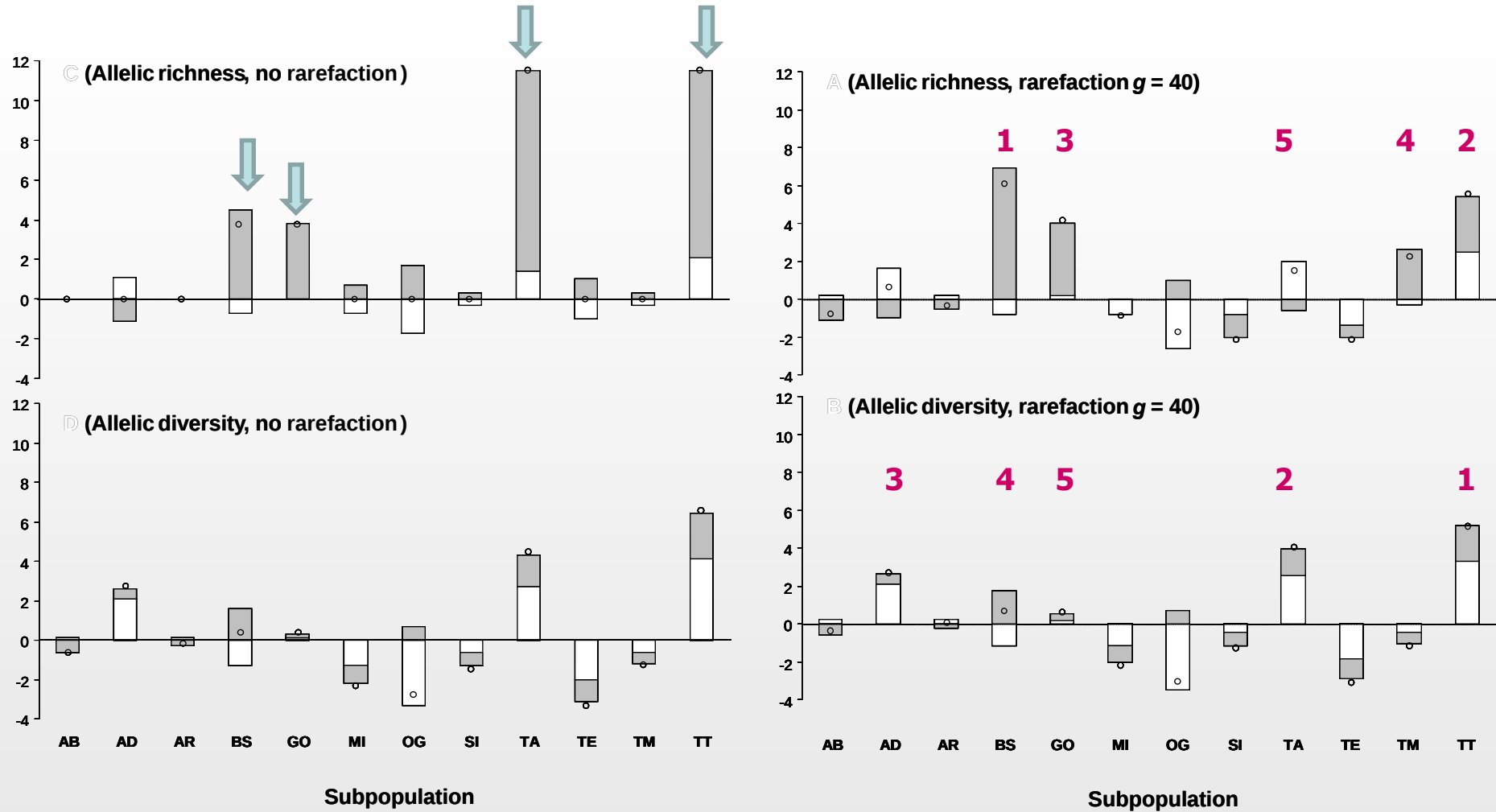


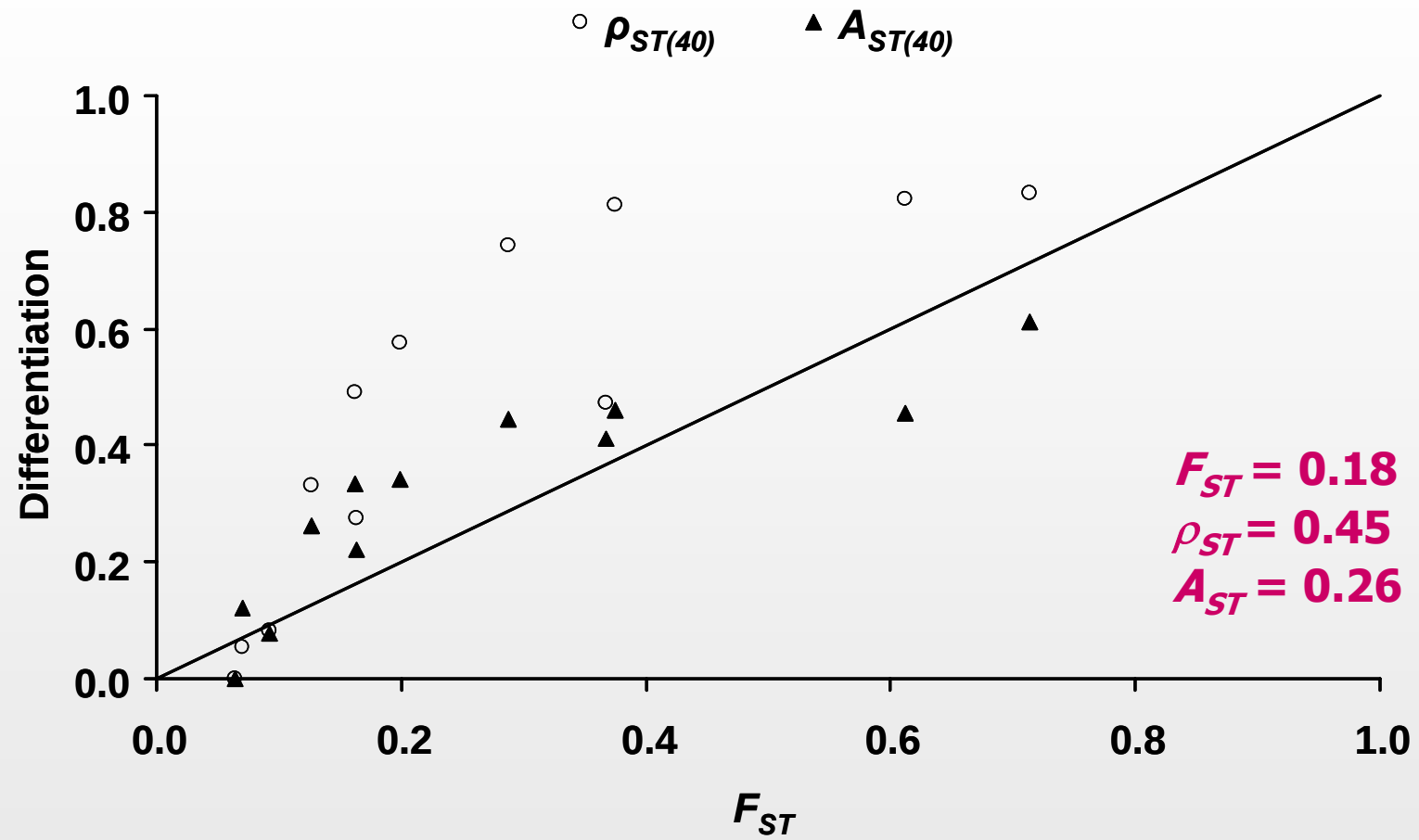
12 populations

12 markers



Contribution (%): ○ Total □ Within-subpopulation ■ Between-subpopulation





1. It has been proposed a partition of allelic diversity into within and between-subpopulations components and, subsequently, an allelic differentiation coefficient, with interest from the point of view of priorisation of populations in conservation.
2. A_{ST} differs from ρ_{ST} because ρ_{ST} depends on the average allelic richness of the subpopulations and the allelic richness of the whole population, whereas A_{ST} depends on the particular arrangement of alleles in the subpopulations.



Thank you for your attention

