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# Is product threshold model better than additive threshold model for studying A.I. result? in sheep

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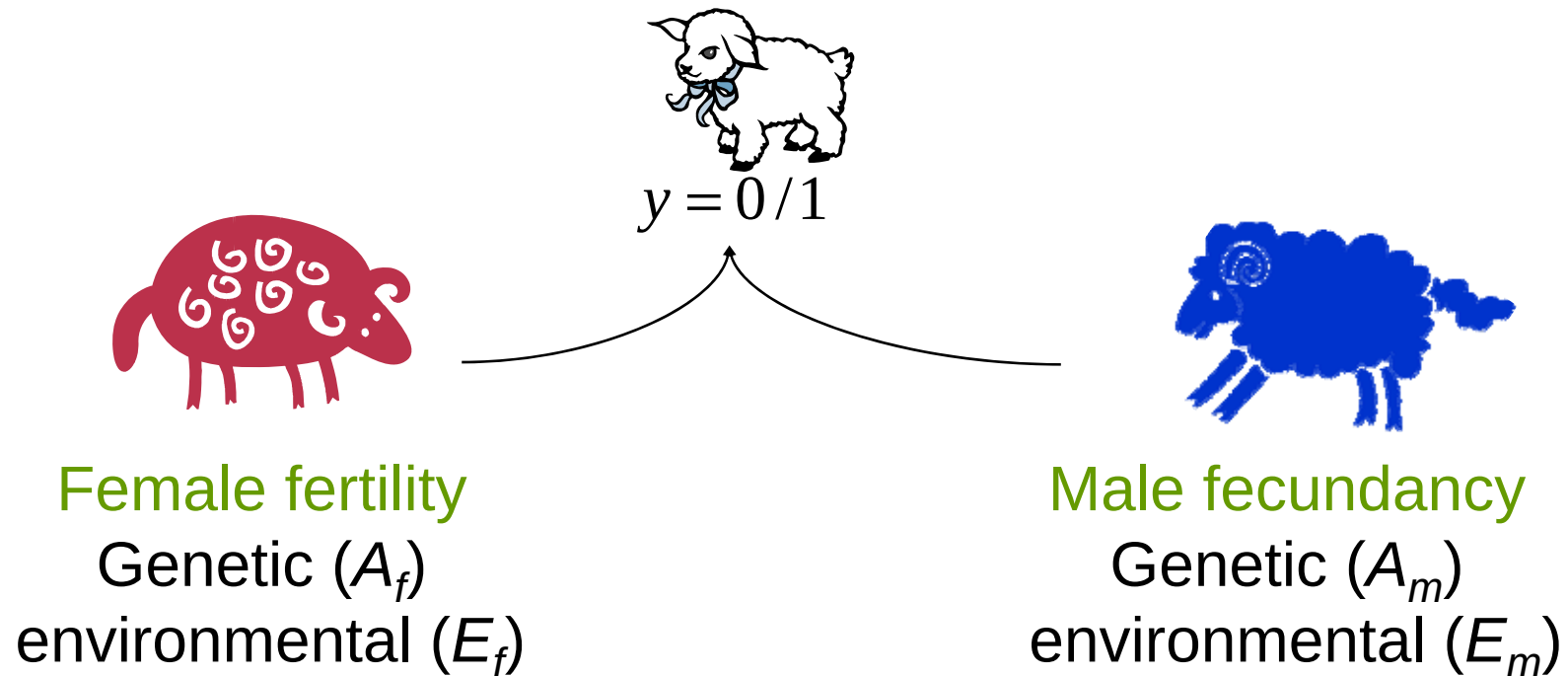
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# Problem



**How to model a binary phenotype  
dependent on 2 individuals ?**

# Possible solution 1

Additive threshold model

$$P(\text{AI success}) = \Phi(\underbrace{A_f + E_f}_{\text{female}} + \underbrace{A_m + E_m}_{\text{male}})$$
$$\Phi(A_f + A_m + E)$$

**Is it the right association ?**

## Possible solution 2

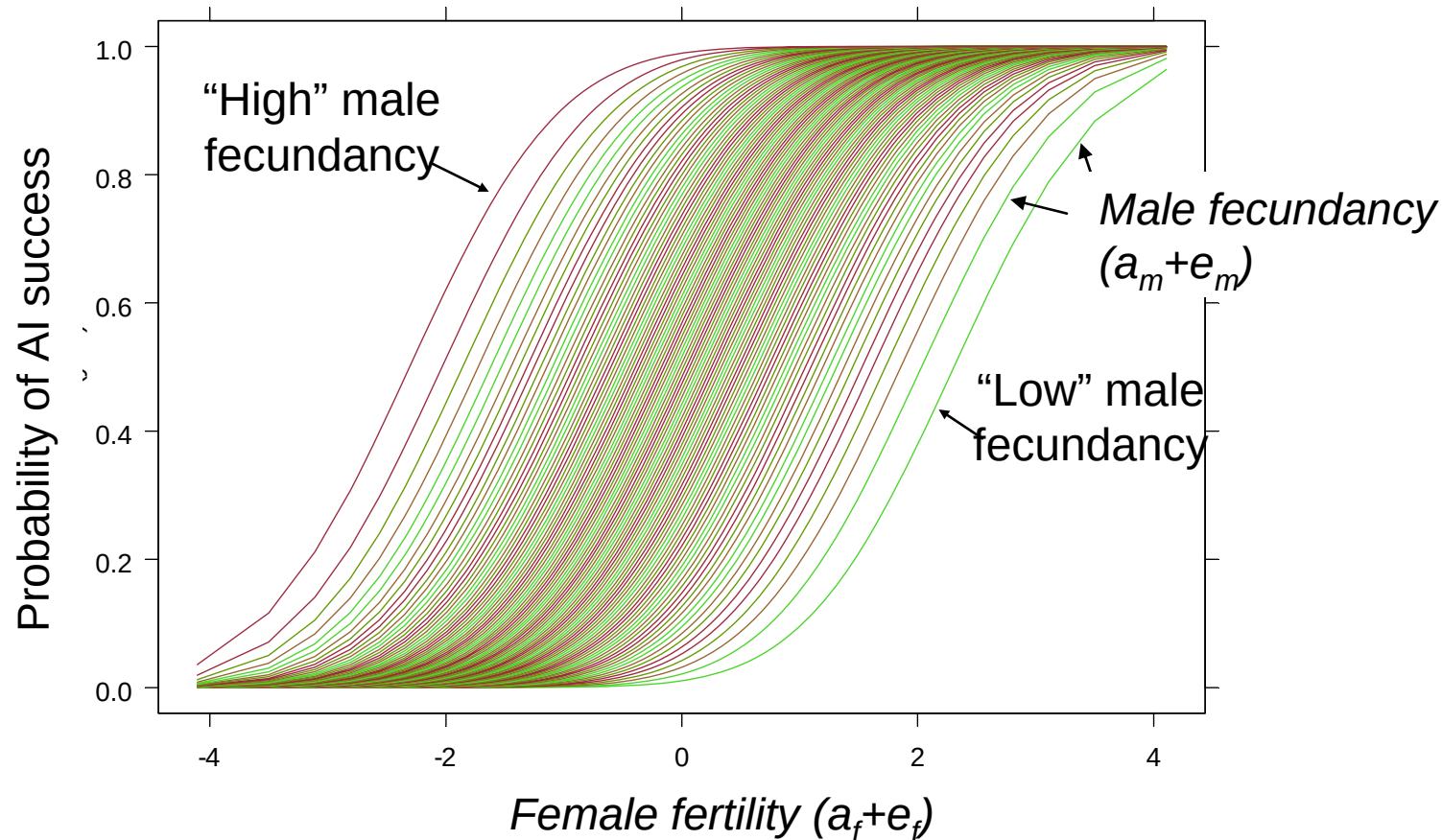
### Additive threshold model

$$P(\text{AI success}) = \Phi\left(\underbrace{A_f + E_f}_{\text{female}} + \underbrace{A_m + E_m}_{\text{male}}\right)$$

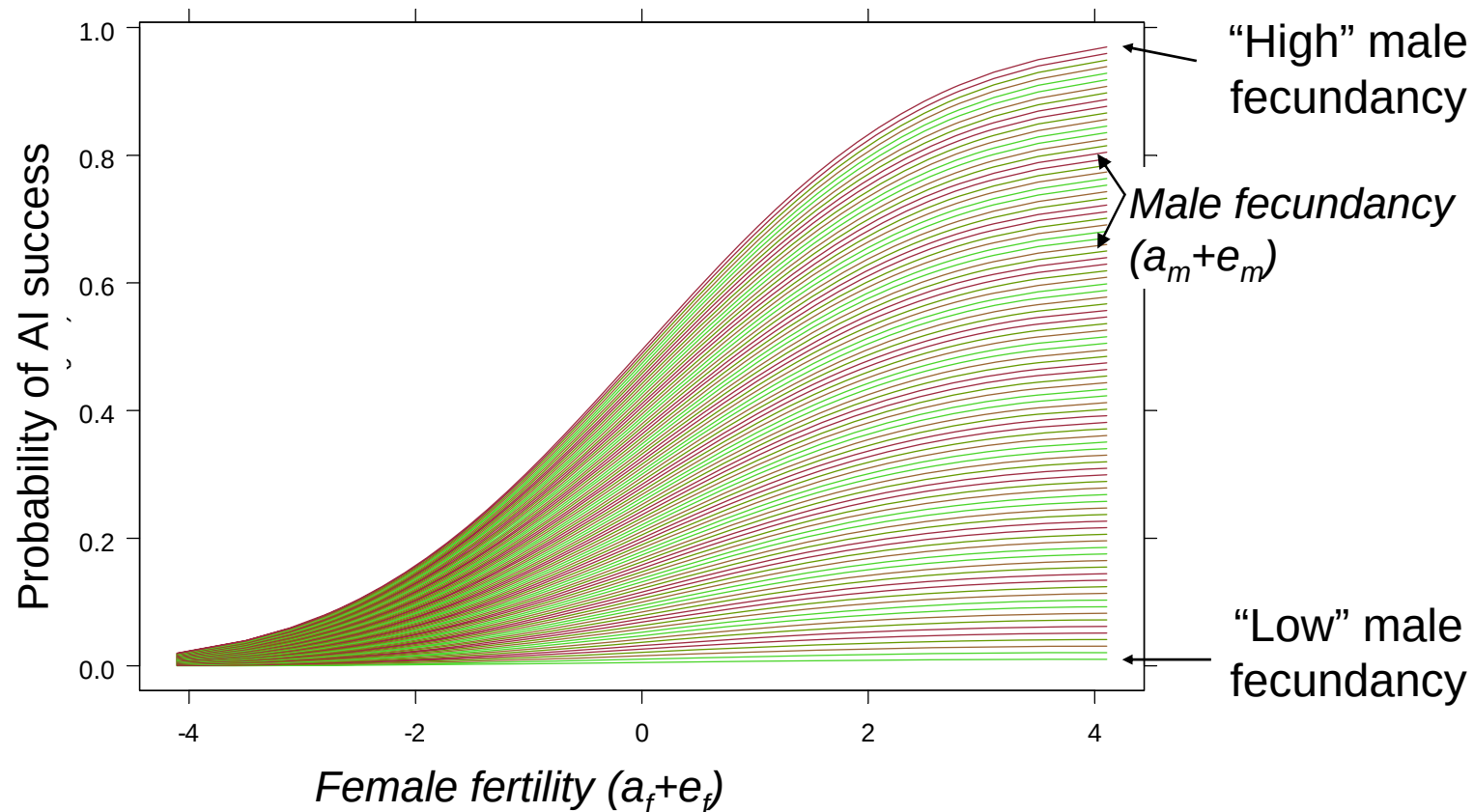
### Product threshold model

$$P(\text{AI success}) = P(\text{female fertility}) \times P(\text{male fecundancy})$$
$$\underbrace{\Phi(A_f + E_f)}_{\text{female}} \times \underbrace{\Phi(A_m + E_m)}_{\text{male}}$$

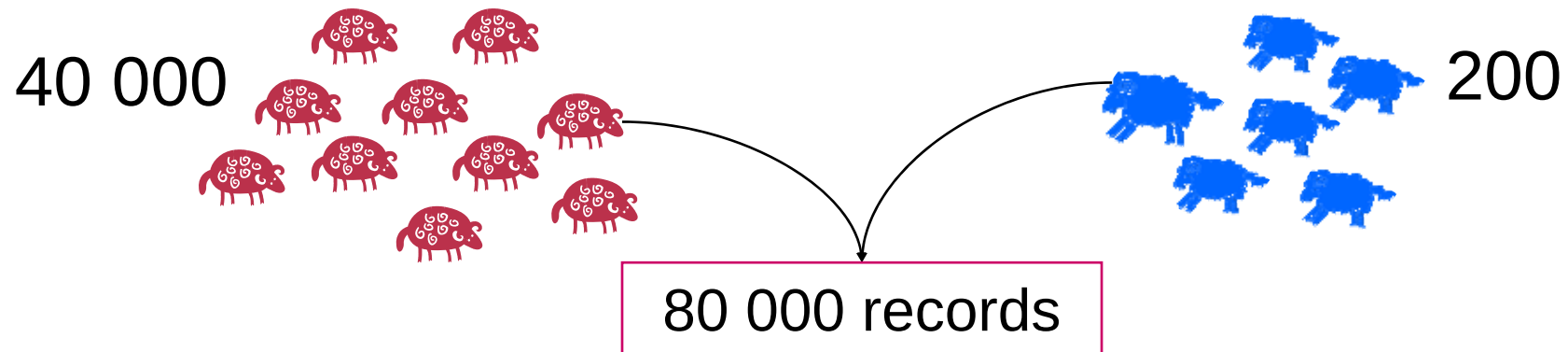
# Consequences of the additive threshold model



# Consequences of the product threshold model



# Simulation design



$$\left. \begin{array}{l} a_f \\ \text{year} \end{array} \right\} P_f \quad P_m \left\{ \begin{array}{l} a_m \\ \text{year} \\ \text{age of the male} \end{array} \right.$$

$$P(\text{AI success}) = 50\%$$





# Parameter estimations

Bayesian approach, Gibbs sampling,  
Modification *TM program* (Andres Legarra)

- Product threshold model

Parameters estimable?

Program works?



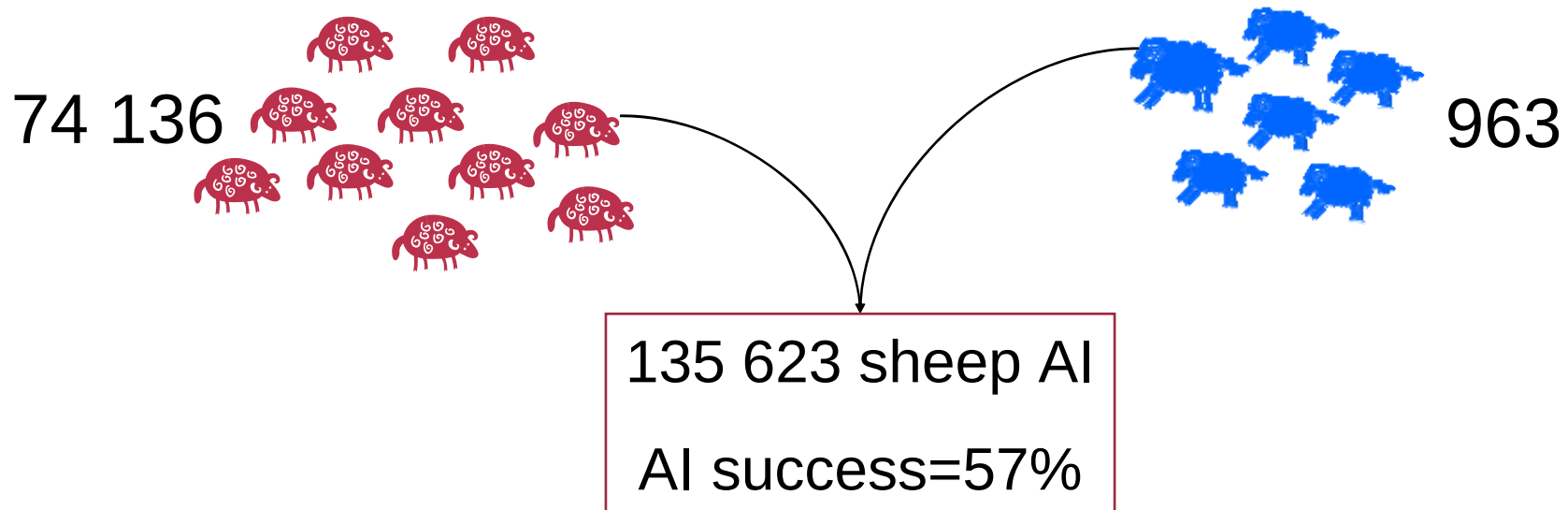
# Good estimations

|                                   | Simulated | Result |                     |
|-----------------------------------|-----------|--------|---------------------|
| Genetic Male fecundancy variance  | 0.25      | 0.25   | [0.21,0.29]         |
| Genetic Female fertility variance | 0.36      | 0.36   | [0.33,0.41]         |
| Genetic correlation               | 0.30      | 0.21   | [0.03,0.41]         |
| year effect                       | Male      | -1.50  | -1.46 [-1.52,-1.41] |
|                                   |           | 0.50   | 0.53 [0.47,0.60]    |
|                                   | female    | 1.50   | 1.54 [1.47,1.63]    |
|                                   |           | 1.00   | 1.00 [0.97,1.04]    |
| Male age effect                   | 2.00      | 1.99   | [1.94,2.03]         |

# Good correlation between BV

| <i>Correlation EBV</i> |                  | EBV  |
|------------------------|------------------|------|
| Real BV                | Male fecundancy  | 0.97 |
|                        | Female fertility | 0.94 |

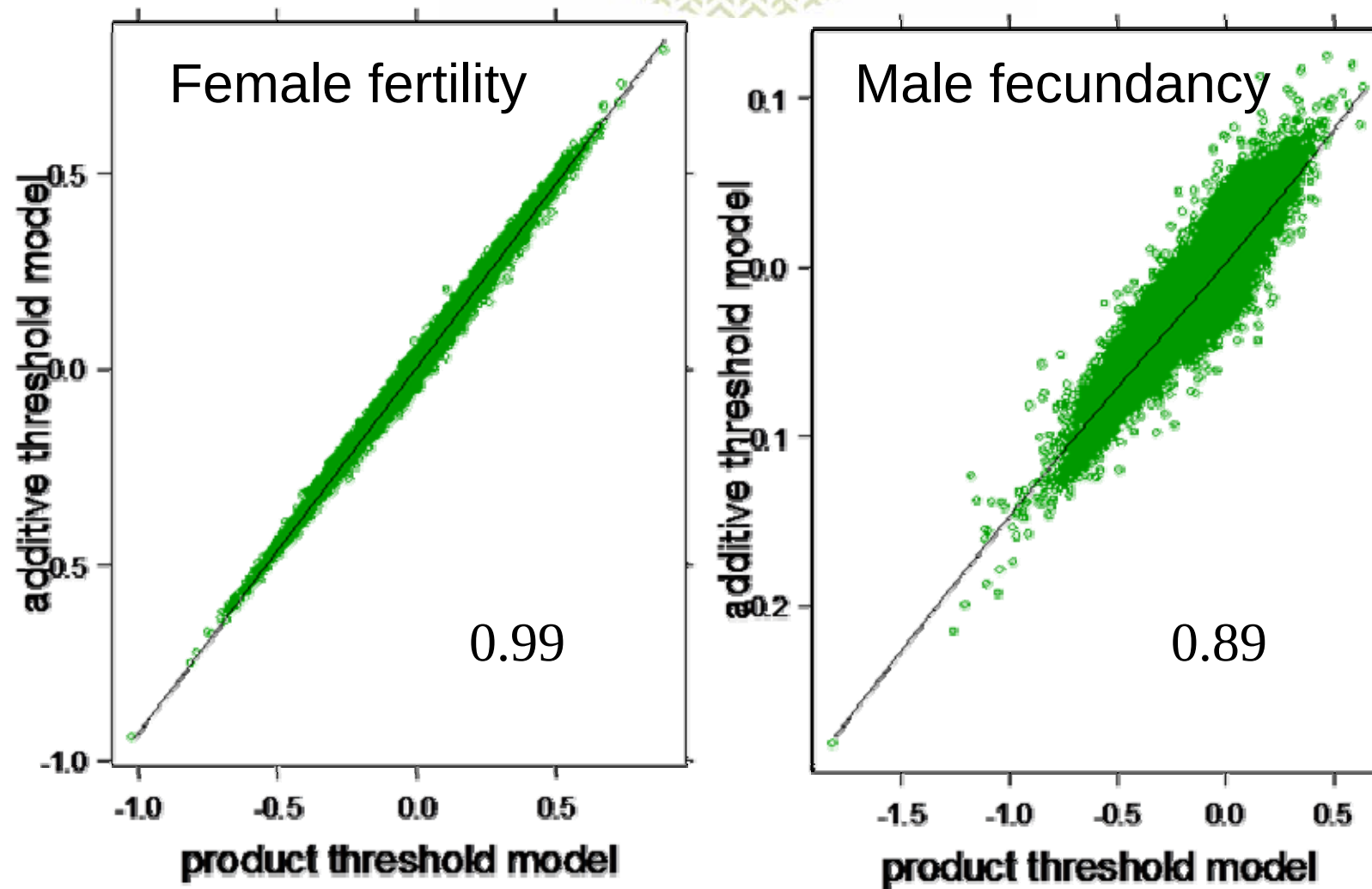
# Field data



## models

- Product threshold model
- Additive threshold model

# Field data: preliminary results



# Discussion / conclusion

## Advantage

- In accordance with biology
- Easy to implement
- Estimate effects for male and female separately

## Disadvantage

- Estimate parameters for the unobserved phenotypes

$$0.75 = 0.87 * 0.87$$

Convergence limit:  
extreme case problem